B.TECH.

THEORY EXAMINATION (SEM–IV) 2016-17
THEORY OF AUTOMATA AND FORMAL LANGUAGES

Time : 3 Hours   *Max. Marks : 100*

Note : *Be precise in your answer. In case of numerical problem assume data wherever not provided.*

SECTION – A

1.   **Explain the following:**   **10 x 2 = 20**

    (a)   Design the DFA that accepts an even number of a's and even number of b's.

   **(b)**   Consider the DFA given below and identify the L accepted by the machine.
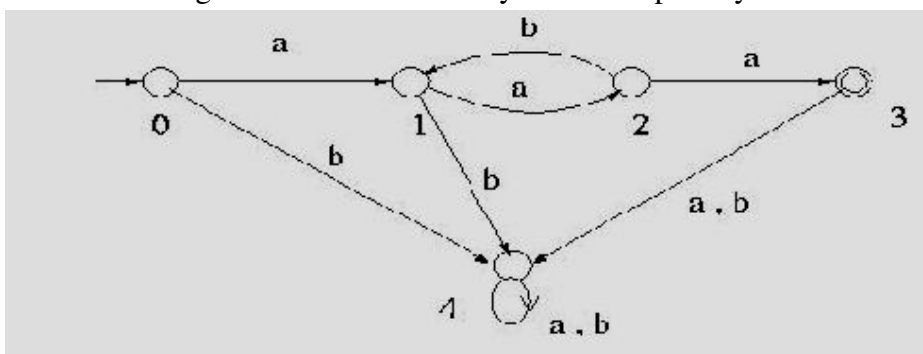
    (c)   State the pumping lemma theorem for regular languages.

   **(d)**   Convert the FA given below to left linear grammar.
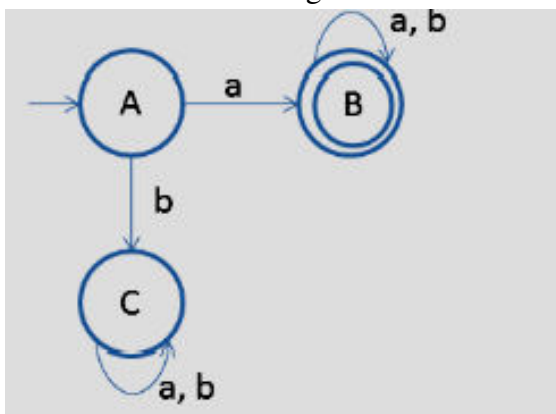
    (e)   Check whether the grammar is ambiguous or not.

            R-> R+R/ RR/ R*/ a / b / c. Obtain the string w = a+b*c

    (f)   S->aB/bA   A->a/aS/bAA   B-> b/bS/aBB. Identify the strings obtained from this grammar.

    (g)   Define PDA. Draw the graphical representation for PDA.

    (h)   Design a PDA which accepts set of balanced paranthesis ({ { } }).

    (i)   Eliminate unit productions in the grammar. S->A/bb A->B/b B->S/a

    (j)   What are checking off symbols?

SECTION – B

2.   **Attempt any five of the following questions:**   **5 x 10 = 50**

    (a)   (i)   Convert the NFA- ε to DFA.
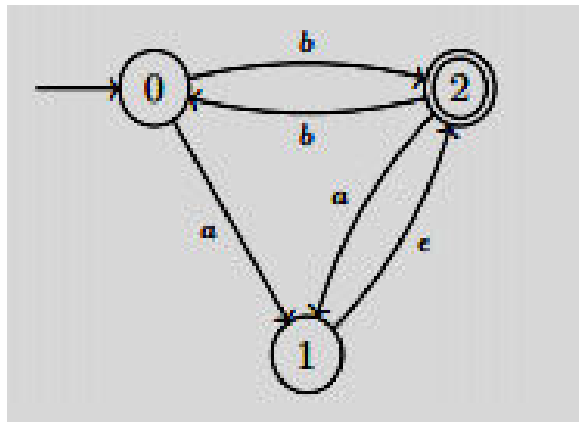
   (ii)   Check with the comparison method for testing equivalence of two FA given below.
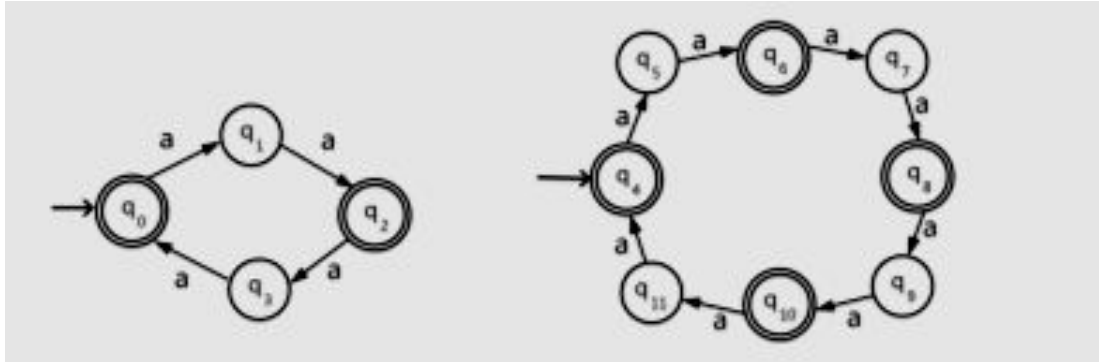
(b) Prove that the compliment, homomorphism and inverse homomorphism, closure of a regular language is regular.

(c) State and prove kleene's theorem with an example.

(d) Consider the grammar with the production S->aSS A->b. Compute the string aababbb with the left most and right most derivation. Draw the derivation tree.

(e) (i) Find out whether the language $L = \{x^n y^n z^n \mid n \geq 1\}$ is context free or not.

    (ii) Construct a PDA that accepts $L = \{ ww^R \mid w = (a+b)^* \}$

(f) (i) Convert the following CFG into CNF

$$S \rightarrow XY \mid Xn \mid p$$
$$X \rightarrow mX \mid m$$
$$Y \rightarrow Xn \mid o$$

    (ii) Convert the following CFG into CNF $\quad S \rightarrow ASA \mid aB, A \rightarrow B \mid S, B \rightarrow b \mid \varepsilon$

(g) Design a TM to recognize all strings consisting of an odd number of α's.

(h) Prove that the halting problem is undecidable.
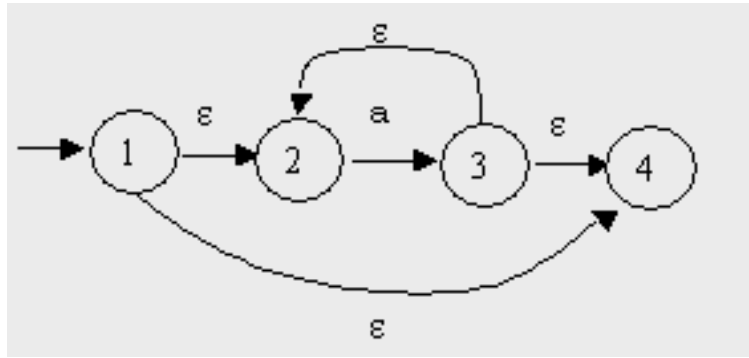
SECTION – C

Attempt any two of the following questions: **2 x 15 = 30**

3. **(a)** Minimize the automata given below
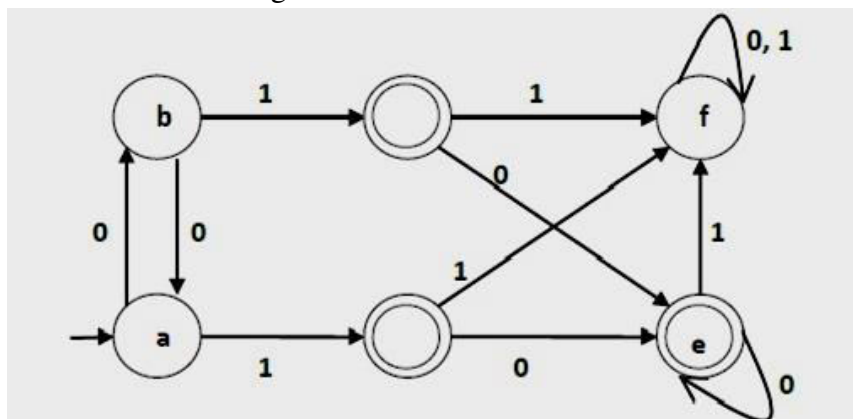
(b) Compute the epsilon- closure for the given NFA. Convert it into DFA.

4. **(a)** Construct PDA to accept $L= \{0^n 1^n \mid n \geq 0\}$

(b) Construct a PDA from the following CFG.

$G = (\{S, X\}, \{a, b\}, P, S)$ where the productions are −

$S \rightarrow XS \mid \varepsilon \,, A \rightarrow aXb \mid Ab \mid ab$

5. **(a)** Prove that single tape machines can simulate multi tape machines.

(b) Design a TM to recognize all strings consisting of an odd number of α's.